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- Knowledge graphs: predict subject-verb-object triples.

Learning a relation between two entities

A relation between users and items (movies). From MovieLens:

| User | Item | Rating | Timestamp |
|------|------|--------|-----------|
| 196 | 242 | 3 | 881250949 |
| 186 | 302 | 3 | 891717742 |
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\widehat{r}_{ui} = predicted rating of user u on item i

Es = set of (u, i, r) tuples in the training set (ignoring timestamp)

Minimize sum squares error:

$$\sum_{(u,i,r) \in Es} (\widehat{r}_{ui} - r)^2$$

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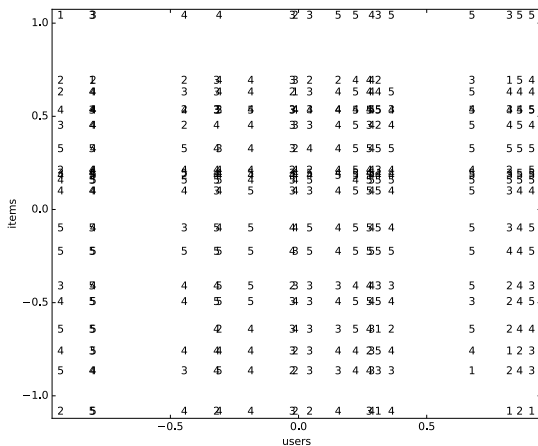
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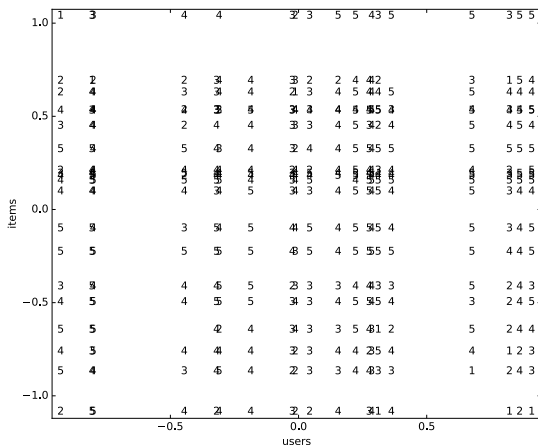
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What pattern would you expect?

- k latent features (Python notation):

$$\widehat{r}_{ui} = \mu + b_1[u] + b_2[i] + \sum_f E_1[u][f] * E_2[i][f]$$

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- Regularize parameters except μ .

- L_2 regularization, minimize:

$$\left(\sum_{(u,i,r) \in E_s} (\widehat{r}_{ui} - r)^2 \right) + \lambda \sum_{\text{parameter } p} p^2$$

L2 regularization

Minimize:

$$\left(\sum_{(u,i,r) \in Es} (\mu + b_1[u] + b_2[i] + \sum_k E_1[u][f] * E_2[i][f] - r)^2 \right) + \lambda \left(\sum_i (b_1[u]^2 + \sum_f E_1[u][f]^2) + \sum_u (b_2[i]^2 + \sum_f E_2[i][f]^2) \right)$$

where λ is a regularization parameter.

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To find minimizing parameters:

- Gradient descent
- Iterative least squares: fix one of E_1 and E_2 ; the problem is ridge regression in the other.

$\mu :=$ average rating

assign $E_1[u][f]$, $E_2[i][f]$ randomly and assign $b_1[i]$, $b_2[u]$ arbitrarily

repeat:

for each $(u, i, r) \in Es$:

$$e := \mu + b_1[i] + b_2[u] + \sum_k E_1[u][f] * E_2[i][f] - r$$

$$b_1[i] := b_1[i] - \eta * e$$

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for each feature k :

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but the average probability is $1/k$, which is not derived from the data.

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All embeddings $E_1[e]$, $E_2[r]$ and $E_3[e]$ are the same length.

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- But, not all relations have same number of negative examples, eg. "*married-to*" vs "*has-streamed*".

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- polyadic decomposition with inverses:

$$\widehat{p}(h, r, t) = \frac{1}{2}(\widehat{pd}(h, r, t) + \widehat{pd}(t, r^{-1}, h))$$

where \widehat{pd} is the prediction from the polyadic decomposition.

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- It learns about each entity; embeddings are used to predict interactions.
- It does not learn general knowledge that can be applied to other populations.