

Learning Objectives - Reinforcement Learning

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- Explain the relationship between decision-theoretic planning (MDPs) and reinforcement learning

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- Explain the relationship between decision-theoretic planning (MDPs) and reinforcement learning
- Implement basic state-based reinforcement learning algorithms: Q-learning

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possible actions
- **Observations** current state of world
immediate reward / punishment
- **Goal** act to maximize accumulated (discounted) reward
- Like decision-theoretic planning, except model of dynamics and model of reward not given.

Reinforcement Learning Examples

- Game -

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- Game - reward winning, punish losing

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Reinforcement Learning Examples

- Game - reward winning, punish losing
- Dog - reward obedience, punish destructive behavior
- Robot - reward task completion, punish dangerous behavior

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- At any time it must decide whether to do.
 - ▶ **explore** to gain more knowledge
 - ▶ **exploit** knowledge it has already discovered

Why is reinforcement learning hard?

- What actions are responsible for a reward may have occurred a long time before the reward was received.
 - ▶ The dog is expected to determine that eating the shoe at the start of the day is what was responsible for it being scolded at the end of the day.

Why is reinforcement learning hard?

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- The long-term effect of an action depend on what the agent will do in the future.
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- The long-term effect of an action depend on what the agent will do in the future.
 - ▶ It might be okay for a robot to create a mess as long as it cleans up after itself.
- The explore-exploit dilemma: at each time should the agent be greedy or inquisitive?

Reinforcement learning: main approaches

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- learn a model consisting of state transition function $P(s'|a, s)$ and reward function $R(s, a)$; solve this as an MDP.
- learn $Q^*(s, a)$, use this to guide action.

Recall: Asynchronous VI for MDPs, storing $Q[s, a]$

(If we knew the model:)

Initialize $Q[S, A]$ arbitrarily

Repeat forever:

- Select state s , action a
- $Q[s, a] := R(s, a) + \gamma \sum_{s'} P(s'|s, a) \left(\max_{a'} Q[s', a'] \right)$

Asynchronous VI for Deterministic RL

initialize $Q[S, A]$ arbitrarily

observe current state s

repeat forever:

 select and carry out an action a

 observe reward r and state s'

What do we know now?

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$Q[s, a] := r + \gamma \max_{a'} Q[s', a']$

$s := s'$

Computing Averages: Temporal Differences

- Suppose we have a sequence of values:

$$v_1, v_2, v_3, \dots$$

and want a running estimate of the average of the first k values:

$$A_k = \frac{v_1 + \dots + v_k}{k}$$

Temporal Differences (cont)

- Suppose we know A_{k-1} and a new value v_k arrives:

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Let $\alpha_k = \frac{1}{k}$, then

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Let $\alpha_k = \frac{1}{k}$, then

$$\begin{aligned}A_k &= (1 - \alpha_k)A_{k-1} + \alpha_k v_k \\ &= A_{k-1} + \alpha_k(v_k - A_{k-1})\end{aligned}$$

“TD formula”

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$$\sum_{k=1}^{\infty} \alpha_k = \infty \text{ and } \sum_{k=1}^{\infty} \alpha_k^2 < \infty.$$

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- Often we use this update with α fixed.
- We can guarantee convergence to average if $\sum_{k=1}^{\infty} \alpha_k = \infty$ and $\sum_{k=1}^{\infty} \alpha_k^2 < \infty$.
- E.g., $\alpha_k = 10/(9+k)$ treats more recent experiences more, but converges to average.

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which can be used in the TD formula giving:

$$Q[s, a] := Q[s, a] + \alpha \left(r + \gamma \max_{a'} Q[s', a'] - Q[s, a] \right)$$

initialize $Q[S, A]$ arbitrarily

observe current state s

repeat forever:

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$s := s'$

Properties of Q-learning

- Q-learning converges to an optimal policy, no matter what the agent does, as long as it tries each action in each state enough.
- But what should the agent do?
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 - ▶ Is this appropriate for a robot interacting with the real world?
 - ▶ An agent can make better use of the data by
 - remember previous experiences and use these to update model (action replay)
 - building a model, and using MDP methods to determine optimal policy.
 - doing multi-step backups
- It learns separately for each state.