Idea: search backwards from the goal description: nodes correspond to subgoals, and arcs to actions.

Search problem:

Nodes are subgoals

- Nodes are subgoals
- ullet There is an arc  $\langle g,g'\rangle$  labeled with action A if
  - $\blacktriangleright$  A achieves one of the assignments in g

- Nodes are subgoals
- There is an arc  $\langle g,g' \rangle$  labeled with action A if
  - A achieves one of the assignments in g
  - g' is a proposition that must be true immediately before action A so that g is true immediately after.

- Nodes are subgoals
- There is an arc  $\langle g,g'
  angle$  labeled with action A if
  - A achieves one of the assignments in g
  - g' is a proposition that must be true immediately before action A so that g is true immediately after.
- The start node is the goal to be achieved.

- Nodes are subgoals
- There is an arc  $\langle g,g'
  angle$  labeled with action A if
  - A achieves one of the assignments in g
  - g' is a proposition that must be true immediately before action A so that g is true immediately after.
- The start node is the goal to be achieved.
- *goal(g)* is true if *g* is a proposition that is true of the initial state.

## Defining nodes and arcs

• A node g can be represented as a set of assignments of values to variables:

$$[X_1 = v_1, \ldots, X_n = v_n]$$

## Defining nodes and arcs

• A node g can be represented as a set of assignments of values to variables:

$$[X_1 = v_1, \ldots, X_n = v_n]$$

This is a set of assignments you want to hold.

• The last action achieves one of the  $X_i = v_i$ ,

$$[X_1 = v_1, \ldots, X_n = v_n]$$

This is a set of assignments you want to hold.

The last action achieves one of the X<sub>i</sub> = v<sub>i</sub>, and does not achieve X<sub>j</sub> = v'<sub>i</sub> where v'<sub>i</sub> is different to v<sub>j</sub>.

$$[X_1 = v_1, \ldots, X_n = v_n]$$

- The last action achieves one of the X<sub>i</sub> = v<sub>i</sub>, and does not achieve X<sub>j</sub> = v'<sub>i</sub> where v'<sub>i</sub> is different to v<sub>j</sub>.
- The neighbor of g along arc A must contain:

$$[X_1 = v_1, \ldots, X_n = v_n]$$

- The last action achieves one of the X<sub>i</sub> = v<sub>i</sub>, and does not achieve X<sub>j</sub> = v'<sub>i</sub> where v'<sub>i</sub> is different to v<sub>j</sub>.
- The neighbor of g along arc A must contain:
  - The prerequisites of action A

$$[X_1 = v_1, \ldots, X_n = v_n]$$

- The last action achieves one of the X<sub>i</sub> = v<sub>i</sub>, and does not achieve X<sub>j</sub> = v'<sub>i</sub> where v'<sub>i</sub> is different to v<sub>j</sub>.
- The neighbor of g along arc A must contain:
  - The prerequisites of action A
  - All of the elements of g that were not achieved by A

$$[X_1 = v_1, \ldots, X_n = v_n]$$

This is a set of assignments you want to hold.

- The last action achieves one of the X<sub>i</sub> = v<sub>i</sub>, and does not achieve X<sub>j</sub> = v'<sub>i</sub> where v'<sub>i</sub> is different to v<sub>j</sub>.
- The neighbor of g along arc A must contain:
  - The prerequisites of action A
  - All of the elements of g that were not achieved by A

it must be consistent = have at most one value for each feature.

 $\langle g, g' \rangle$  is an arc labeled with action A where g is  $[X_1 = v_1, \dots, X_n = v_n]$  and A is an action, if

< □

 $\langle g, g' \rangle$  is an arc labeled with action A where g is  $[X_1 = v_1, \dots, X_n = v_n]$  and A is an action, if •  $\exists i \ X_i = v_i$  is on the effects list of action A

$$\langle g,g'
angle$$
 is an arc labeled with action A where g is  $[X_1=v_1,\ldots,X_n=v_n]$  and A is an action, if

•  $\exists i \ X_i = v_i$  is on the effects list of action A

• 
$$orall j \; X_j = v_j'$$
 is not on the effects list for A, where  $v_j' 
eq v_j$ 

$$\langle g,g'
angle$$
 is an arc labeled with action A where g is  $[X_1=v_1,\ldots,X_n=v_n]$  and A is an action, if

- $\exists i X_i = v_i$  is on the effects list of action A
- $\forall j \ X_j = v'_j$  is not on the effects list for A, where  $v'_j \neq v_j$
- $g' = preconditions(A) \cup \{X_k = v_k \in g : X_k = v_k \notin effects(A)\}$

- $\langle g, g' \rangle$  is an arc labeled with action A where g is  $[X_1 = v_1, \dots, X_n = v_n]$  and A is an action, if
  - $\exists i X_i = v_i$  is on the effects list of action A
  - $\forall j \ X_j = v'_j$  is not on the effects list for A, where  $v'_j \neq v_j$
  - g' = preconditions(A) ∪ {X<sub>k</sub> = v<sub>k</sub> ∈ g : X<sub>k</sub> = v<sub>k</sub> ∉ effects(A)} if it is consistent



< □

- Goal  $G_1$  is simpler than goal  $G_2$  if  $G_1$  is a subset of  $G_2$ .
  - ▶ It is easier to solve [*cs*] than [*cs*, *rhc*].
- If you have a path to node N have already found a path to a *simpler* goal, you can prune the path N.

• You can define a heuristic function that estimates how difficult it is to solve a goal from a state.

 You can define a heuristic function that estimates how difficult it is to solve a goal from a state.
 A heuristic function defined the cost of getting from a state to a (sub)goal. This is the same as a heuristic for the forward planner.

- - L

- You can define a heuristic function that estimates how difficult it is to solve a goal from a state.
   A heuristic function defined the cost of getting from a state to a (sub)goal. This is the same as a heuristic for the forward planner.
- You can use domain-specific knowledge to remove impossible goals, e.g.
  - It is often not obvious from an action description to conclude whether an agent can hold multiple items at any time.

< □

## • Which is more efficient depends on:

The branching factor

## • Which is more efficient depends on:

- The branching factor
- How good the heuristics are

- Which is more efficient depends on:
  - The branching factor
  - How good the heuristics are
- Forward planning is unconstrained by the goal (except as a source of heuristics).
- Regression planning is unconstrained by the initial state (except as a source of heuristics)