Ask-the-user meta-interpreter

% $aprove(G)$ is true if G is a logical consequence of the base-level KB and yes/no answers provided by the user.

$$aprove(true).$$

$$aprove((A \,\&\, B)) \leftarrow aprove(A) \wedge aprove(B).$$

$$aprove(H) \leftarrow askable(H) \wedge answered(H, yes).$$

$$aprove(H) \leftarrow$$
$$\quad askable(H) \wedge unanswered(H) \wedge ask(H, Ans) \wedge$$
$$\quad record(answered(H, Ans)) \wedge Ans = yes.$$

$$aprove(H) \leftarrow (H \Leftarrow B) \wedge aprove(B).$$

Meta-interpreter to collect rules for WHY

% $wprove(G, A)$ is true if G follows from base-level KB, and A is a list of ancestor rules for G.

$$
\begin{aligned}
&wprove(true, Anc).\\
&wprove((A \,\&\, B), Anc) \leftarrow\\
&\quad wprove(A, Anc) \wedge\\
&\quad wprove(B, Anc).\\
&wprove(H, Anc) \leftarrow\\
&\quad (H \Leftarrow B) \wedge\\
&\quad wprove(B, [(H \Leftarrow B) | Anc]).
\end{aligned}
$$

Delaying Goals

Some goals, rather than being proved, can be collected in a list.

- To delay subgoals with variables, in the hope that subsequent calls will ground the variables.
- To delay assumptions, so that you can collect assumptions that are needed to prove a goal.
- To create new rules that leave out intermediate steps.
- To reduce a set of goals to primitive predicates.

Delaying Meta-interpreter

% $dprove(G, D_0, D_1)$ is true if D_0 is an ending of list of delayable atoms D_1 and $KB \wedge (D_1 - D_0) \models G$.

$dprove(true, D, D).$

$dprove((A \,\&\, B), D_1, D_3) \leftarrow$

$\quad dprove(A, D_1, D_2) \wedge dprove(B, D_2, D_3).$

$dprove(G, D, [G|D]) \leftarrow delay(G).$

$dprove(H, D_1, D_2) \leftarrow$

$\quad (H \Leftarrow B) \wedge dprove(B, D_1, D_2).$

Example base-level KB

$$live(W) \Leftarrow$$
$$\quad connected\_to(W, W_1)\ \&$$
$$\quad live(W_1).$$
$$live(outside) \Leftarrow true.$$
$$connected\_to(w_6, w_5) \Leftarrow ok(cb_2).$$
$$connected\_to(w_5, outside) \Leftarrow ok(outside\_connection).$$
$$delay(ok(X)).$$
$$?dprove(live(w_6), [\,], D).$$

Meta-interpreter that builds a proof tree

% $hprove(G, T)$ is true if G can be proved from the base-level KB, with proof tree T.

$hprove(true, true).$

$hprove((A \,\&\, B), (L \,\&\, R)) \leftarrow$

$\quad hprove(A, L) \wedge$

$\quad hprove(B, R).$

$hprove(H, if(H, T)) \leftarrow$

$\quad (H \Leftarrow B) \wedge$

$\quad hprove(B, T).$